

# The rocky ride of the breakeven inflation rates

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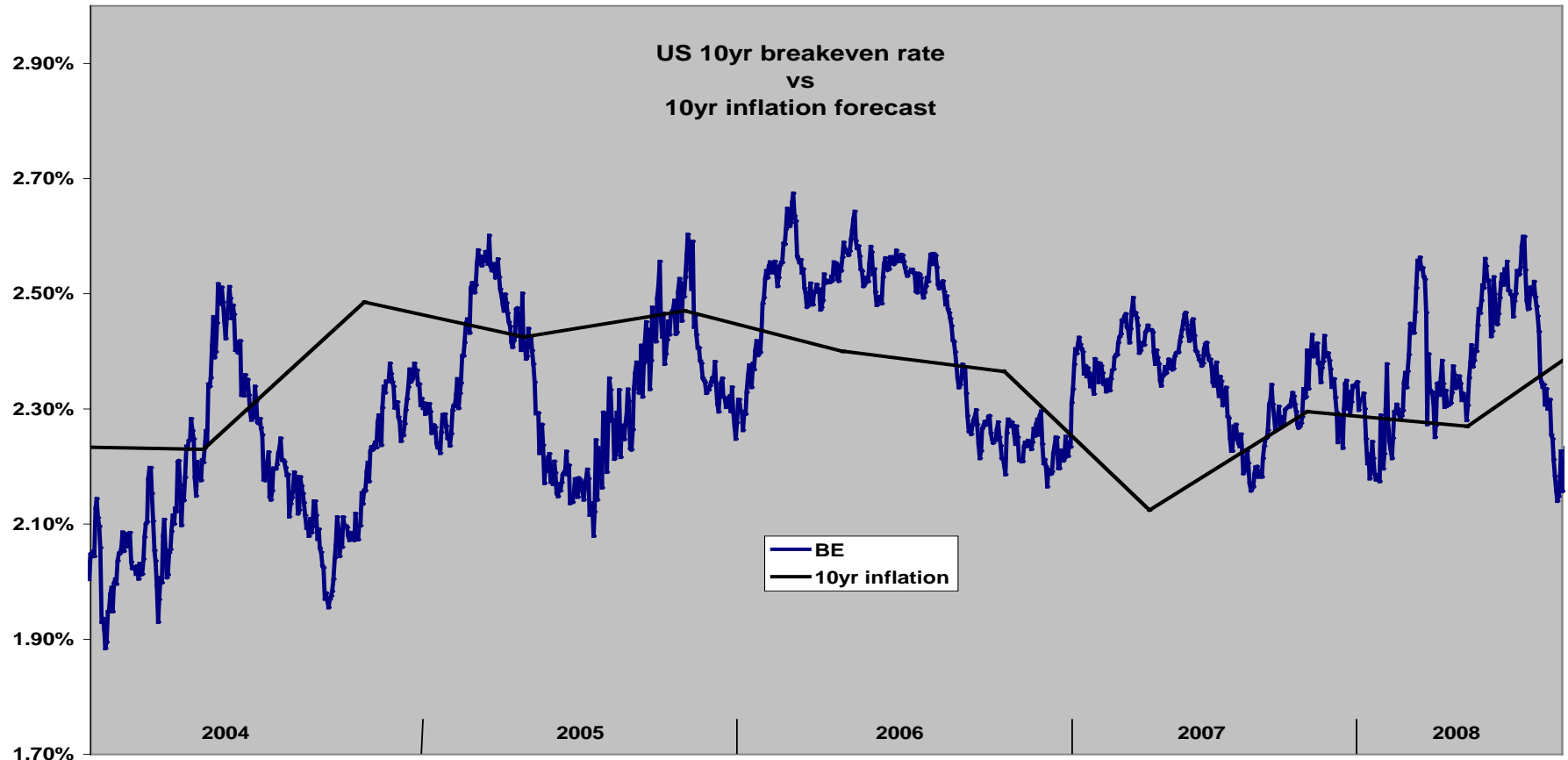
*Venice, June 2009*



# The issuance of **inflation-linked bonds** has given :

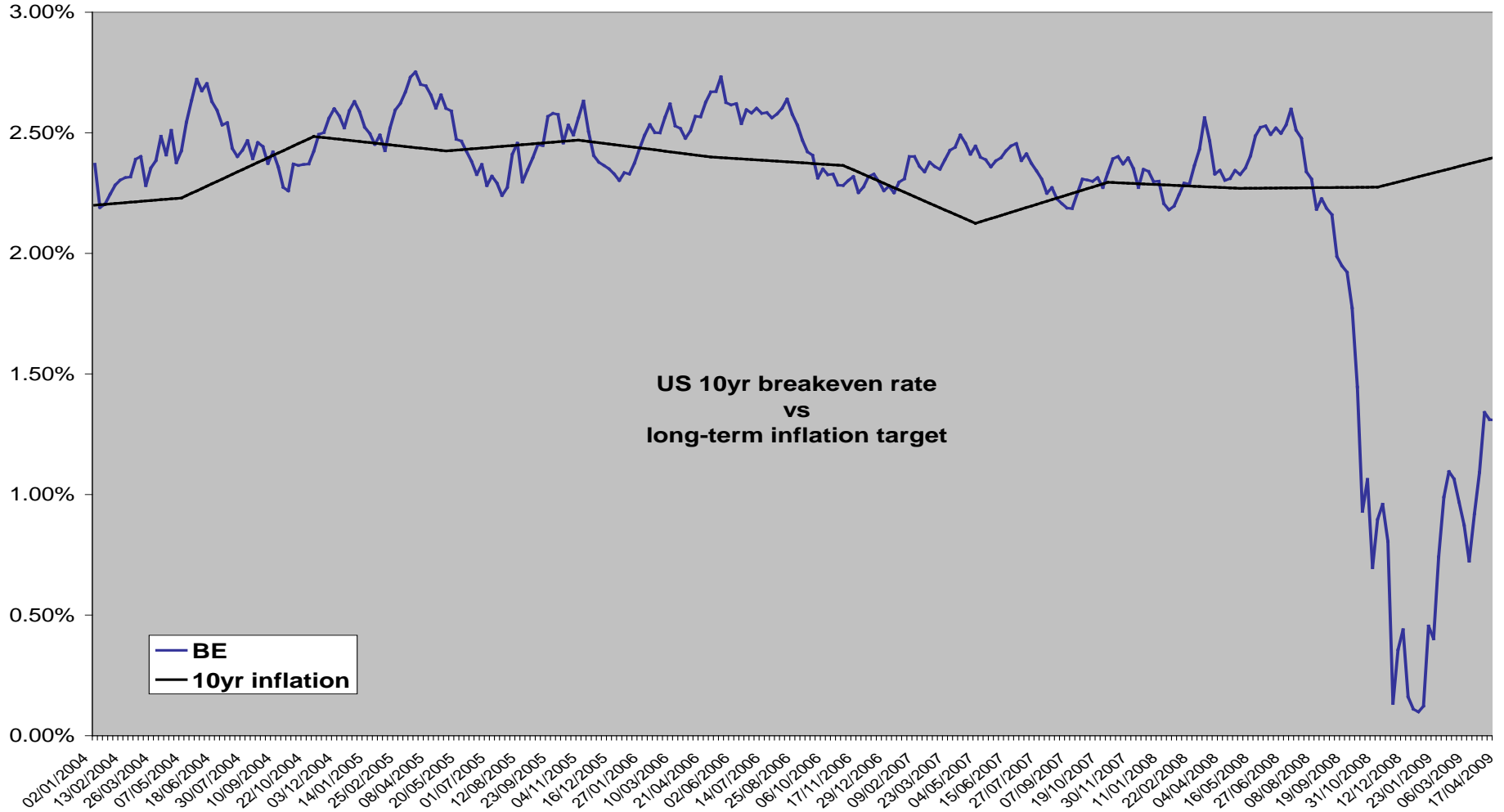
- life to two hitherto theoretical concepts : the **real interest rate** and the nominal-real rate differential called the **breakeven inflation rate**,
- new investment opportunity,
- new risk diversification opportunity,
- feedback to central banks on their monetary policy,
- some thought-provoking surprises ...

# ... breakeven rates go through a rocky ride



- Bernanke (2004) :  
« breakeven inflation rates have proven surprisingly volatile over their short history »

... becoming rockier ...



# ... their co-movements with real rates are surprising ...

- Breakeven rates are systematically correlated with real interest rates in other countries, but **NOT** with the real rate in their own country.

*on weekly data  
2002-2008*

**real rates**

		Australia	Canada	Euro Area	Great-Britain	Sweden	United States
breakeven rates	Australia	0.27	0.19	0.37	0.33	0.41	0.34
	Canada	0.30	-0.06	0.37	0.33	0.29	0.45
	Euro Area	0.20	0.04	-0.18	0.09	0.11	0.13
	Great-Britain	0.20	0.14	0.31	-0.07	0.28	0.29
	Sweden	0.30	0.19	0.43	0.39	0.13	0.37
	United States	0.19	0.10	0.10	0.15	0.13	-0.03

- An investor who buys a US inflation-linked bond (a TIPS) is, as expected, unexposed to the US breakeven rate, yet finds himself exposed to the Canadian breakeven rate movements.

## ... and continue to surprise ...

- Breakeven rates are anti-correlated with real interest rates nearly everywhere.

*on weekly data  
05/2008-04/2009*

**real rates**

	Australia	Canada	Euro Area	Great-Britain	Sweden	United States
<b>breakeven rates</b>	-0.33	-0.37	-0.09	-0.25	-0.33	-0.28
Australia	-0.33	-0.37	-0.09	-0.25	-0.33	-0.28
Canada	0.12	-0.62	0.00	-0.28	0.16	-0.31
Euro Area	0.00	-0.19	-0.55	-0.38	0.12	-0.13
Great-Britain	-0.04	-0.36	-0.17	-0.66	0.29	-0.30
Sweden	0.19	-0.01	0.18	0.13	-0.01	0.06
United States	0.25	-0.38	0.02	-0.14	0.15	-0.59

- The holder of the TIPS is now very exposed to US inflation concerns, while its price reaction to inflation concerns elsewhere has inverted.

# Explanations of the price performance

- For the **excess volatility** of the breakeven inflation rates
  - Consensus up to 2008
  - Views today
- For the **atypical correlation structure**
  - Valid up to 2008
  - Views today

# Explanations of the excess volatility

– up to 2008

The Fisher (1930) equation, decomposing the nominal rate ( $NR$ ) into the real rate ( $RR$ ) and the inflation expectation ( $INF$ ), has been augmented by a time-varying premium variable  $\pi$ , that captures

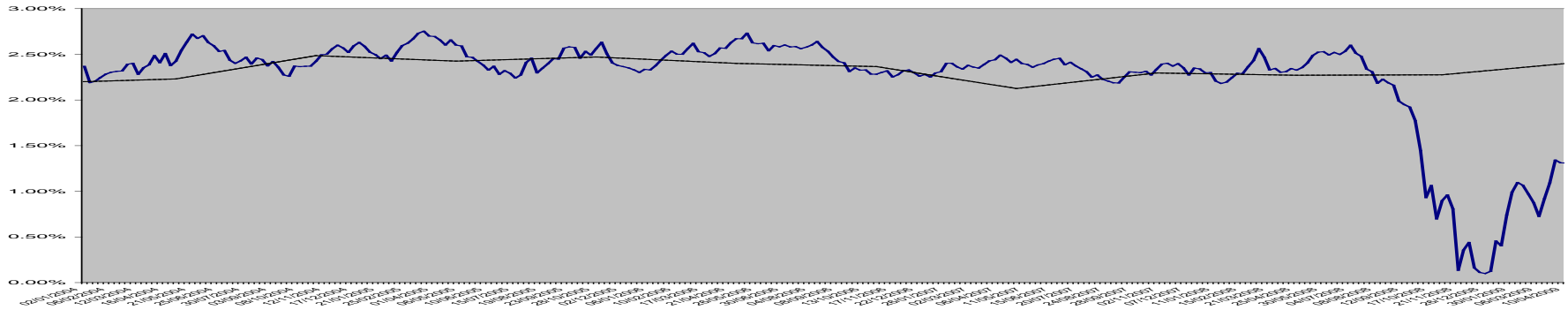
$$NR = RR + INF = RR + BE + \pi$$

- a **liquidity premium** on inflation-linked bonds, according to Shen (2001,2006).
- a **risk premium**, according to Hördahl (2007), Emmons (2000), Evans (1998) and Côté (1996).
- the **seasonality** in consumer prices within the year, according to Ejsing (2007).



# Explanations of the excess volatility

- today



- **Hefty inflation shocks** in 2008

The record levels of the Brent have installed a new fear of inflation and the financial crisis has provoked a fear for deflation thereafter.

- **Collapse of Lehman Brothers**

Leading experts on inflation-linked bonds.

- **Quantitative easing**

Nominal bonds have been bought back massively whereas real bonds have been left untouched.

# Explanations of the atypical correlation structure

## Method of analysis

- Decompose into global and country-specific interest rate movements.

$$BE \begin{matrix} & RR & \\ \begin{bmatrix} 0 & \dots & + \\ : & \ddots & : \\ + & \dots & 0 \end{bmatrix} & = & \begin{matrix} global \\ \begin{bmatrix} ? \\ \end{bmatrix} \end{matrix} + \begin{matrix} country - specific \\ \begin{bmatrix} ? \\ \end{bmatrix} \end{matrix} \end{matrix}$$

- Explain the two components separately.

has changed

has remained unchanged over 2008

# Decomposition of the interest rate movements

- Let  $\Delta BE_{it}$  : the weekly variation of the *BE* in country *i*, analogous for *RR*.

$$\Delta BE_{it} = \beta_i^{BE} * F_t^{BE} + \varepsilon_{it}$$

$$\Delta RR_{it} = \beta_i^{RR} * F_t^{RR} + \eta_{it}$$

- The share of variance explained by the global factor up to 2008

variance share	Australia	Canada	Euro Area	Great-Britain	Sweden	United States
<i>RR</i>	39%	41%	77%	69%	63%	77%
<i>BE</i>	44%	55%	24%	29%	50%	39%

- The betas

betas	Australia	Canada	Euro Area	Great-Britain	Sweden	United States
<i>RR</i>	0.77	0.55	1.19	1.12	0.85	1.47
<i>BE</i>	1.26	1.19	0.59	0.69	1.15	1.05

# Decomposition of the correlation matrix

- Let  $\Gamma$  be the correlation matrix under study and  $S_{BE}$  a composed diagonal matrix of variance shares ( $S_{RR}$  analogous) :

$$S_{BE} = \begin{bmatrix} S_{BE}^{glob} & \\ & S_{BE}^{spec} \end{bmatrix}$$

- Then  $\Gamma$  can be decomposed as :

$$\Gamma = S_{BE} \circ \begin{bmatrix} \Gamma^{glob\ glob} & \Gamma^{glob\ spec} \\ \Gamma^{spec\ glob} & \Gamma^{spec\ spec} \end{bmatrix} \circ S_{RR}^T$$

# The decomposed correlation matrix\* :

$$\begin{bmatrix} \Gamma^{glob\ glob} & \Gamma^{glob\ spec} \\ \Gamma^{spec\ glob} & \Gamma^{spec\ spec} \end{bmatrix} =$$

\*on weekly data  
**2002-2008**

$$\begin{pmatrix} \begin{bmatrix} .48 & .48 & .48 & .48 & .48 & .48 \\ .48 & .48 & .48 & .48 & .48 & .48 \\ .48 & .48 & .48 & .48 & .48 & .48 \\ .48 & .48 & .48 & .48 & .48 & .48 \\ .48 & .48 & .48 & .48 & .48 & .48 \\ .48 & .48 & .48 & .48 & .48 & \{.48\} \end{bmatrix} & \begin{bmatrix} .11 & -.19 & .02 & -.03 & -.02 & .00 \\ .11 & -.19 & .02 & -.03 & -.02 & .00 \\ .11 & -.19 & .02 & -.03 & -.02 & .00 \\ .11 & -.19 & .02 & -.03 & -.02 & .00 \\ .11 & -.19 & .02 & -.03 & -.02 & .00 \\ .11 & -.19 & .02 & -.03 & -.02 & \{.00\} \end{bmatrix} \\ \begin{bmatrix} .12 & .12 & .12 & .12 & .12 & .12 \\ .10 & .10 & .10 & .10 & .10 & .10 \\ -.19 & -.19 & -.19 & -.19 & -.19 & -.19 \\ -.02 & -.02 & -.02 & -.02 & -.02 & -.02 \\ .10 & .10 & .10 & .10 & .10 & .10 \\ -.26 & -.26 & -.26 & -.26 & -.26 & \{-.26\} \end{bmatrix} & \begin{bmatrix} -.08 & .04 & .00 & .00 & .19 & -.05 \\ -.05 & -.43 & -.02 & -.04 & -.10 & .25 \\ .16 & .10 & -.60 & .07 & .12 & .15 \\ -.01 & .09 & .21 & -.57 & .18 & .16 \\ -.04 & .05 & .16 & .14 & -.45 & .02 \\ .12 & .21 & .02 & .18 & .12 & \{-.33\} \end{bmatrix} \end{pmatrix}$$

# Synthesis of the decomposition exercise

- Ignoring the (small) cross-terms and ignoring the fact correlations don't exactly add, we obtain schematically :

$$BE \begin{matrix} & RR & & \\ \begin{bmatrix} 0 & .. & + \\ : & \ddots & : \\ + & .. & 0 \end{bmatrix} & = & \begin{matrix} global \\ \begin{bmatrix} + & .. & + \\ : & : & : \\ + & .. & + \end{bmatrix} & + & \begin{matrix} country - specific \\ \begin{bmatrix} - & .. & 0 \\ : & \ddots & : \\ 0 & .. & - \end{bmatrix} \end{matrix} \end{matrix} \quad \text{up to 2008}$$

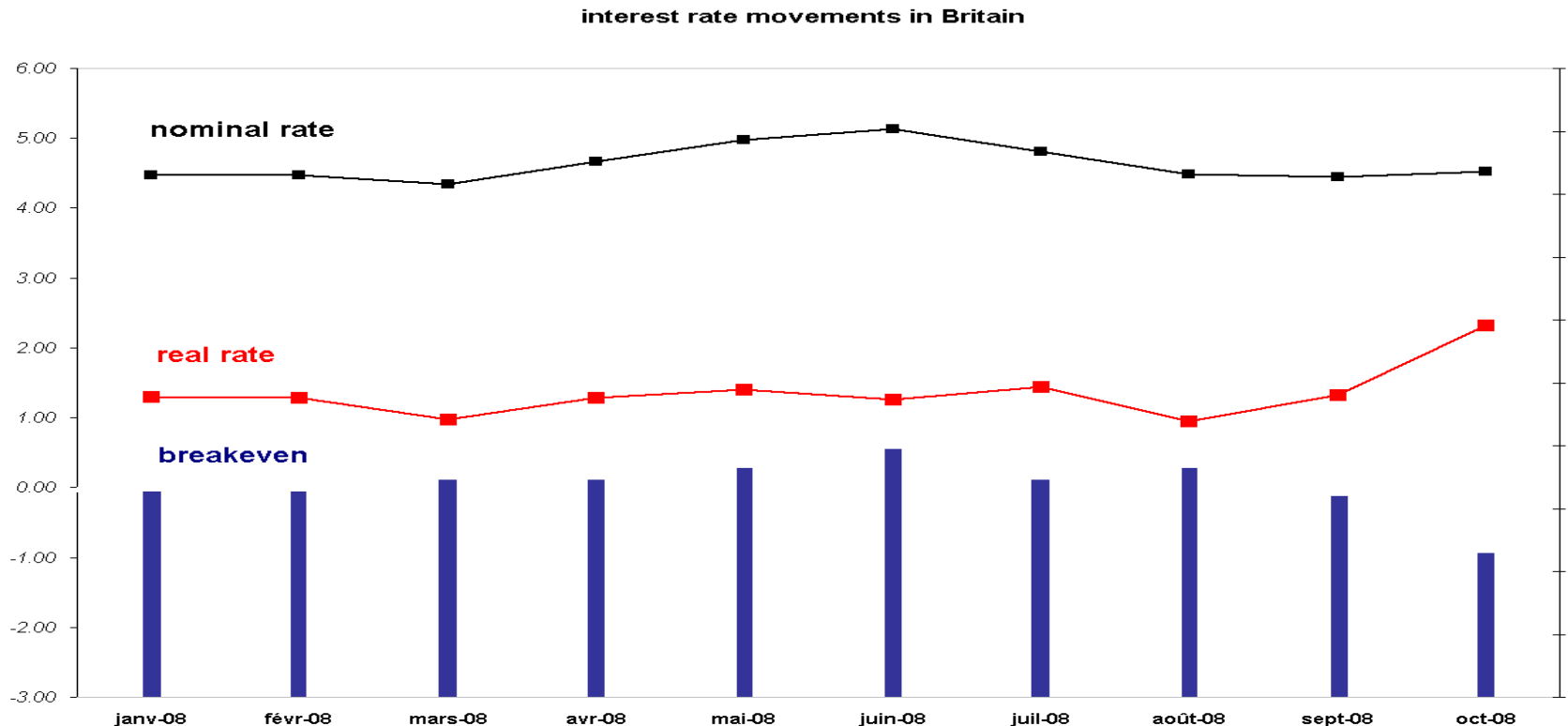
$$BE \begin{matrix} & RR & & \\ \begin{bmatrix} -- & .. & - \\ : & \ddots & : \\ - & .. & -- \end{bmatrix} & = & \begin{matrix} global \\ \begin{bmatrix} - & .. & - \\ : & : & : \\ - & .. & - \end{bmatrix} & + & \begin{matrix} country - specific \\ \begin{bmatrix} - & .. & 0 \\ : & \ddots & : \\ 0 & .. & - \end{bmatrix} \end{matrix} \end{matrix} \quad \text{over last year}$$

# Synthesis of the decomposition exercise

- Three observations :
  1. The country-specific breakeven inflation rate moves against the country-specific real interest rate.
  2. The correlation between the global breakeven - and the global real rate movements has been significantly positive for fifteen years,
  3. ... and is significantly negative since one year.

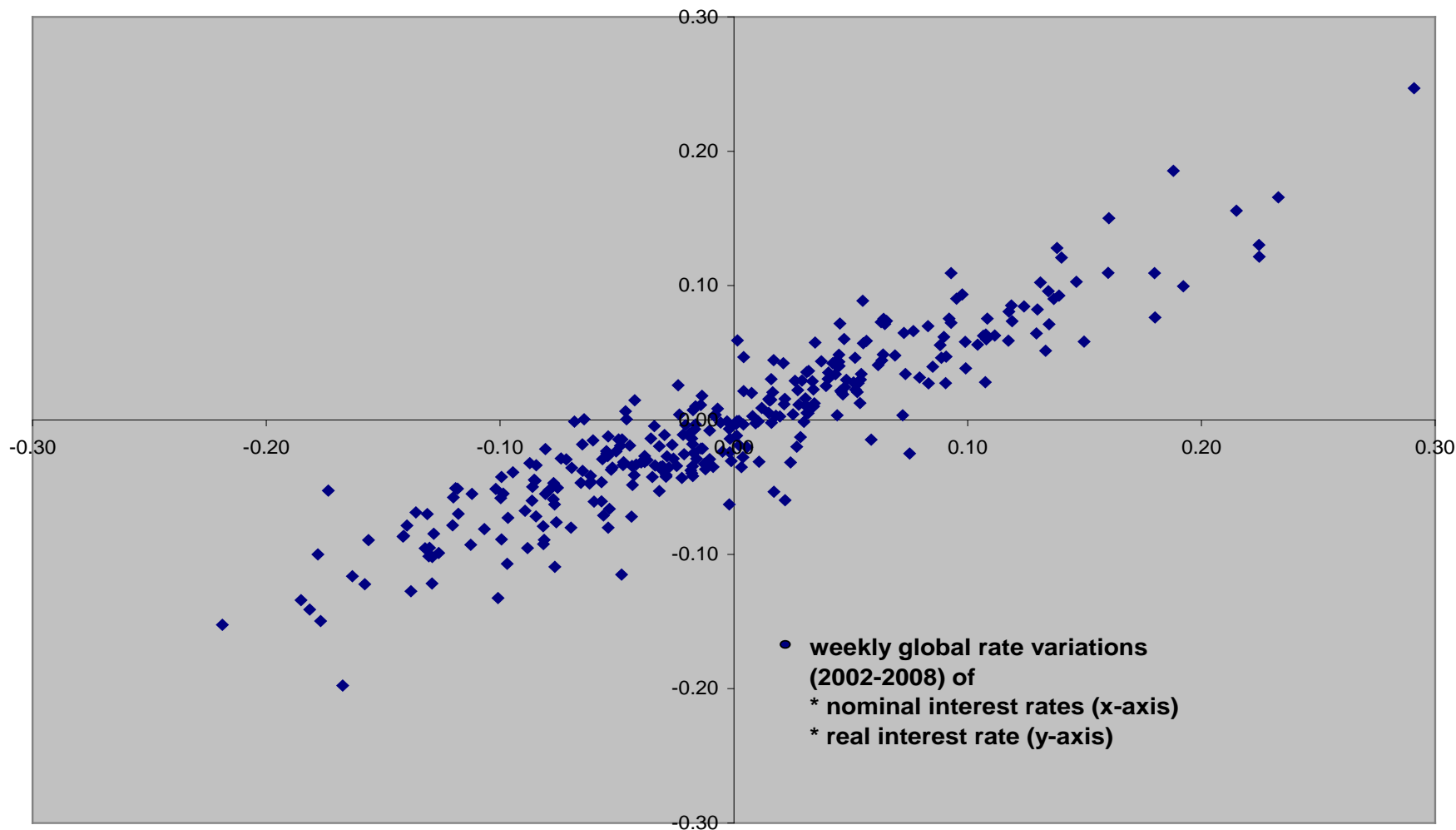
# 1. The local *BE* moves against the local *RR* when ...

- ... a move of the local real rate is not in phase with a move of the local nominal rate. This typically occurs when the *RR* moves for local market-related reasons.





## 2. Fifteen years of *beta effect*\*



\*described in the Barclays Capital handbook

# The beta effect

- In theory (according to Fisher) :

impulse	response	result
'pure' inflation shock	<i>NR</i> moves alone	correlation between <i>BE</i> and <i>RR</i> zero
shock without impact on inflation (e.g. technological shock)	<i>NR</i> and <i>RR</i> move with the same amplitude	

- In practice :

2. A beta of 0.7 observed practically every week for fifteen years.

3. A chaotic beta since one year.

→ A lot remains to be learned on the interaction between inflation and the real economy !

# Conclusion

- *The rocky ride of the breakeven inflation rates\** :  
a high volatility and an untypical correlation structure with real interest rates
- due to
  - market-related factors
  - interaction between inflation and the real economy
- Direct consequences
  - Hinders the assessment of central banks' credibility.
  - The new performance and risk diversification opportunity need to be treated with care.

**\*Published in the Economics Bulletin October 2008**

# Appendix : the Japanese experience

